

Quiz 3A, Calculus I  
Dr. Graham-Squire, Spring 2013

Name: Key

8:22  
8:24  
2

1. (5 points) Use implicit differentiation to find  $y'$  for the equation

$$\frac{d}{dx} \left( \frac{\tan y}{e^x} + 8 = x^3 \right)$$

$$\Rightarrow \frac{\sec^2 y \cdot y' \cdot e^x - (\tan y) e^x}{(e^x)^2} + 0 = 3x^2 \quad \left. \vphantom{\frac{\sec^2 y \cdot y' \cdot e^x - (\tan y) e^x}{(e^x)^2} + 0 = 3x^2}} \right\} 3.5$$

$$\Rightarrow \frac{\sec^2 y \cdot y'}{e^x} - \frac{\tan y}{e^x} = 3x^2$$

$$\frac{\sec^2 y \cdot y'}{e^x} = 3x^2 + \frac{\tan y}{e^x}$$

$$y' = \frac{e^x}{\sec^2 y} \left( 3x^2 + \frac{\tan y}{e^x} \right)$$

1.5

2. (5 points) Find the derivative:

$$\frac{d}{dx} (\cos(e^{3x}))$$

$$= -\sin(e^{3x}) \cdot e^{3x} \cdot 3$$

$$= -3 \sin(e^{3x}) \cdot e^{3x}$$

Quiz 3B, Calculus I  
Dr. Graham-Squire, Spring 2013

Name: Key

1. (5 points) Find the derivative:

$$\frac{d}{dx}(\sin(e^{4x}))$$

$$= \cos(e^{4x}) \cdot e^{4x} \cdot 4$$



2. (5 points) Use implicit differentiation to find  $y'$  for the equation

$$\frac{d}{dx} \left( x^2 - 5 = \frac{\cot y}{e^x} \right)$$

$$2x = \frac{-\csc^2 y \cdot y' \cdot e^x - \cot y \cdot e^x}{(e^x)^2}$$

multiply  
 $e^{2x}$  to other  
side

$$2x \cdot e^{2x} = -\csc^2 y \cdot e^x \cdot y' - e^x \cot y$$

$$2x e^{2x} + e^x \cot y = -\csc^2 y \cdot e^x \cdot y'$$

$$\frac{2x e^{2x} + e^x \cot y}{-\csc^2 y \cdot e^x} = y'$$